Monte Carlo Event Generators

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General Introduction: Principles of MC Generators Event Simulation 1 Hadronization > Dynamics of Confinement Hadronic (pp, pA, AA) Collisions > "Collective Phenomena" New Discoveries > New Ideas

Overview

Perturbative Aspects \leftrightarrow Amplitude Calculations *Perturbative Uncertainties*

Event Simulation 2

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The objective of science

Measure the measurable, and make the unmeasurable measurable.

It seems there is some doubt whether Galileo actually said this.

What has philosophy got to do with measuring anything?

Galileo, *Concerning the New Star (1606)*

(It's the mathematicians you have to trust, and they measure the skies like we measure a field.)

Do measurements ⇔ Learn about Nature

Elementary Fields & Parameters Lagrangians & QFT Perturbation Theory **# of Observed Events**

(Typically) Very Large Backgrounds

Detector Signals Reconstructions

Do measurements ⇔ Learn about Nature

Need precise and detailed relations + Lots of interesting physics on the way

(Typically) Very Large Backgrounds

Connecting theory and experiment

HARD-PROCESS SKELETONS: *Example:* $gg \to t\bar{t}$ + Resonance decays + DETECTOR SIMULATIONS + TRIGGERS + RECONSTRUCTION

⇒ Physics Analysis

…

MPI

+ RADIATIVE CORRECTIONS + MPI + CR + HADRONISATION, … ⁺ HADRON (& *τ*) DECAYS

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Figure from [arXiv:2203.11601](https://arxiv.org/abs/2203.11601)

MC Event Generators

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Foundational Principles of MC Event Generators

1. Divide and Conquer

Split the problem into (many) simpler pieces

2. Knowledge is Power

The simpler pieces are given by **Mathematical Factorisations**

+ The loss of perturbation theory in the nonperturbative regime does not imply a total loss of predictivity!

3. God plays dice

We'll do the same!

Perturbative Infinities

Hard LHC collisions contain 100s of particles Need (differential) σ_{pp} for that number of "legs"

Help! Some of them are hadrons! — Non-perturbative

And/or have small opening angles

And/or are "soft"

- + Phase Space $\propto \prod_{i=1}^{100}$ *i*=1 d^3p_i $2E_i$
-

How would *you:*

1 — *Divide et Impera* Caesar

Construct, square, and integrate 100-leg amplitudes (with a lot of IRdivergent + non-pert. structure) over 300-dimensional phase spaces?

➤ break it down!

Big

2 — *Scientia Potentia Est*

- Some Important Factorisations:
- Factorisation of Long-Distance $\mathsf{QCD}\Longrightarrow \mathsf{Can}$ use Perturbation Theory
- Narrow-Width Limit \Longrightarrow Resonance & Hadron production and decay
- Soft and Collinear Factorisation in Gauge Theories \Longrightarrow Iterative FSR & ISR
- + Well-Designed Observables E.g., IR-safe & -sensitive, ratios vs yields, etc.
- Give data to ML and let it work out the transfer function(s)? If the algorithm misses any of the factorisations (or conservations laws), would you trust it? In principle, the data contains the laws. But features differ by orders of magnitude, many are quasi-fractal, … In MCEGs, some laws may of course also be implemented imperfectly But physical basis can be discussed, learned from, and in principle systematically improved How to use ML for interpretation? For *us* to learn. *What* are we looking at?

Driven by differential (e.g., DGLAP) evolution equations, dP/dQ2, as function of resolution scale; from Q_{HARD} to $Q_{HAD} \sim 1$ GeV

Hard Process & Decays:

Use process-specific (N)LO matrix elements (e.g., $gg \rightarrow H^0 \rightarrow \gamma \gamma$) \rightarrow Sets "hard" resolution scale for process: Q_{HARD}

ISR & FSR (Initial- & Final-State Radiation):

Nonperturbative modeling of partons \rightarrow hadrons transition Strings or clusters; followed by hadron and *τ* decays

3 — Most gods play dice; Fate plays chess. Pratchett

Physics Separation of time scales > Factorizations | Maths

→ Can split **big** problem into many (nested) pieces + **make random choices** (MC)² ~ like in nature

 $\mathcal{P}_{\text{event}} = \mathcal{P}_{\text{hard}} \otimes \mathcal{P}_{\text{dec}} \otimes \mathcal{P}_{\text{ISR}} \otimes \mathcal{P}_{\text{FSR}} \otimes \mathcal{P}_{\text{MPI}} \otimes \mathcal{P}_{\text{Had}} \otimes \ldots$

MPI (Multi-Parton Interactions)

Protons contain lots of partons \rightarrow can have additional (soft) parton-parton $interactions \rightarrow Additional (soft)$ "Underlying-Event" activity

Hadronisation

The Physics of Event Generators

- \bigcap Hard Interaction
- Resonance Decays
- MECs, Matching & Merging
- \blacksquare FSR
- \blacksquare ISR*
- **QED**
- **Weak Showers**
- **Hard Onium**
- Multiparton Interactions
- \Box Beam Remnants*
- \boxtimes Strings
- \boxtimes Ministrings / Clusters
- **Colour Reconnections**
- **String Interactions**
- Bose-Einstein & Fermi-Dirac
- **Primary Hadrons**
- Secondary Hadrons
- Hadronic Reinteractions
- $(*:incoming$ lines are crossed)

The Physics of Event Generators

14

Confilherherie in Infort Genergy collisions

dynamical process to ensure partons **(quarks and gluons)** become **confined** within hadrons In high-energy processes, need a

i.e. a non-perturbative parton -> nadron i **parton → hadron map**

Model requirements ➢ Colour neutralisation \triangleright Dynamical mapping to on-shell hadrons

Requirement #1: Colour Neutralisation

of confinement is that partons are **coloured** The point of confinement is that partons are coloured A **physical** model needs two or more partons to create **colour-neutral** objects

ce, compute **potential energy** $V(R)$ of a **colour-singlet** $q\bar{q}$: as function of the distance, R, between the q and \bar{q} : On lattice, compute **potential energy** $V(R)$ of a **colour-singlet** $q\bar{q}$ **state** as function of the distance, R , between the q and \bar{q} :

 \mathcal{L}_A and \mathcal{L}_A and \mathcal{L}_A and \mathcal{L}_A and \mathcal{L}_A and \mathcal{L}_A and \mathcal{L}_A

\triangleright Strings form between partons that form overall **colour-singlet** states **states**

Strings!! ➢ The point of confinement is that partons are **coloured** → a physical model needs Long Wavelengths > 10-15 m Colour neutralisation what physical ph two or more partons to create **colour neutral** objects **Require colour neutralisation:** Colour neutralisation

 $\overline{1}$ $\overline{1}$ $\overline{1}$ 'h " Modelled by analogy with "Schwinger Mechanism" in QED

In addition to the long-range behavior of the confidential confining \mathbf{r}_i potential it is only in the interest to investigate it is ul t_{max} are results. In Fig. 6(a) \sim 1. on energies \gtrsim 1 gev $^{-}$ on energies \lesssim 1 dev High separation energies $≥$ 1 GeV

 $\sum_{i=1}^n$ \rangle regime \rangle string br le (hunoir crootion). \implies String Breaks (by pair creation):

Who gets confined with whom?

A corresponding event record from PYTHIA, up to the second gluon emission

 2 *(constrained by fits to measured hadron spectra)* \mathbf{f} 3 strv'' "Left-right symmetry" \Longrightarrow FF constrained to a form with **two free parameters**, $a \& b$ f

Requirement #2: on-shell hadrons

Observation: All string breaks are **causally disconnected** (➣ independent modulo entanglement from common origin)

Lund(*z*) ∝ 1 *z* $(1 - z)^a$ $\exp\left(-\frac{b(m_h^2 + p_{\perp h}^2)}{t}\right)$ *z*)

Supresses high *z* Supresses low *z*

[See, e.g., [Amoroso et al., JCAP 05 \(2019\) 007](https://arxiv.org/abs/1812.07424)]

Peter Skands \overline{P}

- Lorentz invariance \Longrightarrow string breaks can be leftover string, considered in *any order*.
	- Exploit this to split off "outermost" hadron either from left or right (randomly) — **iteratively!**
	- Hadron *h* takes a fraction z of the quark momentum
	- **Probability distribution** in $z \in [0,1]$ parametrised by **Fragmentation Function**, $f_{\text{Lund}}(z, Q_{\text{HAD}}^2)$

Gluon Kinks: The Signature Feature of the Lund Model

T S OF GEV AND STRUCK

Alternative: **The Cluster Model** — Used in HERWIG & SHERPA

Alternative to strings: S^{\bullet}

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20

10^3 10^4 σ $\left(p \geq p \right)$ vs p Tmin TOŦEM σ_{inel}

 $\alpha_{\rm s}$ =0.130 NNPDF2.3LO

 α _s=0.135 CTEQ6L1

Hadron Collisions → Multi-Parton Interactions

Protons are composite

One proton = **beam** of partons

Interpretation: *σ*parton-parton(*p* ⊥) *σ*hadron-hadron $\sim \langle n \rangle$ _{parton}—parton</sub> (\hat{p}_\perp)

(Regulated at low \hat{p}_\perp by IR cutoff ~ colour screening)

+ dσ_{parton–parton is dominated by *t*-channel gluon} exchange: **diverges for** $\hat{p}_{\perp} \rightarrow 0$ GeV ̂

➜ Multiple Parton-Parton Interactions (MPI)

≈ poor man's saturation 1

\sim 10 0 100 0 150 100 110 Γ 0 0 101 0 Γ 6 0 0 151 1 ↔ cut pomerons in Regge Theory

0 5 10 15 20

∝

αs(*p*⊥)

t

with Impact-parameter dependence

Δ Brief History of MPI (in PYTHIA) the hardest scattering of an event at xTl. For each impact parametering of an event at xTl. For each impact pa
The hardest scattering of an event at xTl. For each impact parametering of an event at a state of an event at **A Brief History of MPI** (in PYTHIA)

Separately, the probability of the probability of \overline{S} in the probability of this should like the probability that the probability of the probability that the event
In the event of the probability that the event of the even 1987 [Sjöstrand & van Zijl, Phys.Rev.D 36 (1987) 2019]

Pythia 8 — **Interleaved** Evolution

2005 [Sjöstrand & PS, [Eur.Phys.J.C 39 \(2005\) 129](https://arxiv.org/abs/hep-ph/0408302)] **Interleave MPI & ISR** evolutions in one common sequence of pt ➜ ISR & MPI "compete" for the available x in the proton remnant. 2011 [\[Corke & Sjöstrand, JHEP 03 \(2011\) 032\]](https://arxiv.org/abs/1011.1759) Also include **FSR** in interleaving

~ Fine-graining of all event structure above hadronization scale in one common sequence of quantum mechanical resolution ∝ p_{\perp}

Confinement in *pp* Collisions

MPI or cut pomerons \Rightarrow lots of coloured partons's cattered into final state Who gets confined with whom?

Each has a colour ambiguity $\sim 1/N_C^2 \sim 10\,\%$

- E.g.: **random triplet** charge has 1/9 chance to be in singlet state with random antitriplet:
	- $3 \otimes \overline{3} = 8 \oplus 1$,
	- $3 \otimes 8 = 15 + 6 + 3$, etc.

Many charges \rightarrow Colour Reconnections* (CR) more likely than not $n_{\rm MPI}$

Expect Prob(no CR) $\propto \left(1-\frac{1}{N_C^2}\right)$

Example (from arXiv:2203.11601) $pp \to t\bar{t}$ (all-jets) cecierelle eelberreeleel Marie Pierre ${\rm d}\hat\sigma_0$ leeelle armonto MPIJ

(And do other things happen? Emergent dynamics?)

***):** in this context, QCD CR simply refers to an ambiguity beyond Leading N_C, known to exist. The term "CR" can also be used more broadly.

"Parton Level" (Event structure before confinement)

When many string configurations are possible, assume nature picks the one with smallest potential energy \sim "string length"

String-length minimisation and <pT>(Nch)

25

[See also Ortiz et al., Phys.Rev.Lett. 111 (2013) 4, 042001]

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QCD @ LHC ≻ Lots of New Discoveries! $\mathsf{QCD} \not\cong \mathsf{LHC} \not\simeq \mathsf{LOIS}$ universe transformation

Regard tension k as an emergent quantity (not fundamental strings)

May depend on (invariant) time *τ*? *E.g.*, hot strings which cool down [\[Hunt-Smith & PZS EPJ C 80 \(2020\) 11](https://arxiv.org/abs/2005.06219)]

May depend on environment? (e.g., other strings nearby) Two approaches (so far) within Lund string-model context: **Colour Ropes** [Bierlich et al. 2015] + several more recent **Close-Packing** [Fischer & Sjöstrand 2017] + Work in progress with L. Bernardinis & V. Zaccolo (Trieste)

Non-Linear String Dynamics? Strangeness, Enhancem

28

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What about Baryon Number?

Types of string topologies:

String Submission Codebases Fragmentation of String Junctions

Assume Junction Strings have same properties as ordinary ones (u:d:s, Schwinger p_T , etc) \triangleright No new string-fragmentation parameters

The Junction Baryon is the most "subleading" hadron in all three "jets".

Generic prediction: low pT

A Smoking Gun for String Junctions: Baryon enhancements at low p_T

[Sjöstrand & PS, [NPB 659 \(2003\) 243\]](https://arxiv.org/abs/2309.01557) [[+ Altmann & PS, JHEP 07 \(2024\) 238](https://arxiv.org/abs/2404.12040)]

Colour Reconnections on String Junctions were those due to the raw-yield extraction, the statistical uncertainties on the e"ciency and **Colour Reconnet in this of string Junctions** be correlated, except the branching ratio uncertainties, which were treated as partially correlated

[Christiansen & PS 2015, Altmann & PS 2024]

Next Steps: put it all together (+ "A*ltmann mechanism" for diquark disruption in octet fields)* See how close we can get to describing light, strange, and heavy-flavour mesons + baryons in pp + Lund group developing extensions/applications to heavy-ion collisions! **Fig. 1:** Left: Prompt Λ⁺ ^c and D⁰ *p*T-differential cross section in pp collisions and in p–Pb collisions r**t Steps:** put it all together (+ "Altmann mechanism" for diquark disruption in octet fields) \blacksquare with theoretical predictions (see text for details). Statement for details for details in details for details systematic uncertainties are shown as boxes, and the bin widths are shown as horizontal bars.

Lots of recent activity ! Also in PYTHIA Led by Jyväskylä & Lund

Heavy-Ion Physics

Disclaimer: I am not an expert

- Also for HI, there are of course event generators E.g., ANGANTYR, EPOS, HIJING, JEWEL, QGSJET, SIBYLL, …
- Another big class of models: **statistical hadronization**
- Differ in how much detail you aim for, how multi-differential and/or eventby-event you want to be able to go …
	- You may want to focus on macroscopic properties, not the microphysics
	- Or you may want to pursue a microscopic description, without all macroscopic aspects
- Most of us specialise, but I don't think the point is to pick a winner As a physicist, I'd like to understand *both:* what are the macroscopic properties? what is the microphysics? How do the former emerge from the latter? Which paradigms are compatible / incompatible? How to form **clear** conclusions from **data?**

Core-corona picture in EPOS

Beyond Strings — QGP? The Corona Solution (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) (2007) 11th MCnet School July 2017 Lund # Klaus Werner # Subatech, Nantes186 11th Mc \sim 11th Mcnet School July 2017 Lund \sim Subatech, Nant \sim Subatech, Nant \sim 12th Mcnet School July 2017 Lund \sim The Core–Corona Solution (2007) Core-corona picture in EPOS

Currently most realistic complete approach for $pp \leftrightarrow pA \leftrightarrow AA?$ The core-corona solution [Werner 2007]: mix discrete strings with continuous QGP Frontig infodentiality complete approach for pp. (Mp. 1971). C The core-corona solution [Werner 2007]: **mix** discrete **strings** with continuous QGP Currently most realistic "complete" approach: $\overline{}$ Gribov-Regge approach = (Many) kinky strings
Strings = (Many) kinky strings = (Many) kinky strings = (Many) kinky strings = (Many) kinky strings = (Many) k Cantenty most reansul complete d Gurrantly most raalistic complat correlity inost realistic complete app

decay and statistical decay (*n*₀) statistical decay (*n*) statistical decay core => hydro => statistical decay (*µ* = 0) core => hydro => statistical decay $(\mu = 0)$ corona => string decay

high mult pp low mult pp

Allows smooth transition between string and hydro descriptions. Implemented in **EPOS MC** Qualitatively agrees with ALICE strangeness data (but too steep rise with multiplicity?) SHS. Implemented in EPOS MC \mathbf{R} were respectively in the set of \mathbf{R} (2007) \mathbf{R} AIIOWS SITIOO Allows smooth trans Qualitatively agrees with ALICE, but too steep rise.

The Core–Corona Solution (2007)

$115₁$

rings with continuous Qur \mathbf{G}

The Corona Solution (2007) \sim Corona Solution (2007) \sim Corona Solution (2007) \sim Corona Solution (2007) \sim

Conversely: Collective flow from strings? (without QGP) • Colour-electric fields classical force. • Let *g* determine fraction in field, and normalization *N* is given: 2 /2*R*²

magnetic flux)

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Colour-electric fields ➜ Classical force

Pythia for Cosmic Rays ↔ Corsika 8 A prising framework for the collision in

with Applications to Cosmic Rays",

Based on 2 articles by Marius Utheim & TS:

- "A Framework for Hadronic Rescattering in pp Collisions", Eur. Phys. J. C80 (2020) 907, arXiv:2005.05658
- "Hadron Interactions for Arbitrary Energies and Species,
- Eur. Phys. J. C82 (2022) 21, arXiv:2108.03481

+ Extension with ANGANTYR (→incoming nuclei) > PYTHIA 8.313

- Models arbitrary hadron–hadron collisions at low energies.
- Models arbitrary hadron-p/n collisions at any energy.
- \bullet Initialization slow, \sim 15 minutes, \star but thereafter works for any hadron–p/n at any energy, and \star initialization data can be saved, so only need to do once.
- o The ANGANTYR nuclear geometry part used to extend to hadron-nucleus at any energy.
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- Native $C++$ simplifies interfacing PYTHIA $8 \leftrightarrow$ CORSIKA 8. So far limited comparisons with data.

Extra Slides

 $\langle n_{\text{ch}} \rangle \approx c_0 + c_1$ In E_{cm} , \sim Poissonian multiplicity distribution

(Note on the Length of Strings)

In Spacetime:

String tension ≈ 1 GeV/fm → a 50-GeV quark can travel 50 fm before all its kinetic energy is transformed to potential energy in the string. Then it must start moving the other way.

(→ "yo-yo" model of mesons. Note: string breaks → several mesons)

The MC implementation is formulated in momentum space Lightcone momenta $p_{\pm} = E \pm p_z$ along string axis → Rapidity (along string axis) and p_\perp transverse to it $y =$ 1 2 $\ln\left(\frac{E+p_z}{E}\right)$ $E - p_z$ ◆ = 1 2 $\ln \left(\frac{(E+p_z)^2}{E^2} \right)$ $E^2 - p_z^2$ ◆

Particle Production: Scaling in $z \implies$ flat in rapidity (long. boost invariance) "Lightcone scaling"

Particle Composition: Impact on Jet Energy Scale

- Variation largest for gluon jets For $E_T = [30, 100, 200]$ GeV Max JES variation = **[3%, 2%, 1.2%]**
- Fraction of jet E_T carried by baryons (and kaons) varies significantly
	- Reweighting to force similar baryon and kaon fractions
	- Max variation → [1.2%, 0.8%, 0.5%]
	- Significant potential for improved Jet Energy Scale uncertainties!
- Motivates Careful Models & Careful **Constraints**
	- Interplay with advanced UE models
	- In-situ constraints from LHC data
	- Revisit comparisons to LEP data

ATL-PHYS-PUB-2022-021

ATLAS PUB Note

29th April 2022

[Dependence of the Jet Energy Scale on the Particle](https://cds.cern.ch/record/2808016/files/ATL-PHYS-PUB-2022-021.pdf) of the Particle on the Particle on the Particle Dependence of the Jet Energy Scale on the Particle Content of Hadronic Jets in the ATLAS Detector Simulation

Content of Hadronic Jets in the ATLAS Detector Simulation in Monte Carlo simulations of the particle types and spectra within jets is $\frac{1}{5}$ to the true jet energy kaons and baryons in the jet. Model differences observed for jets initiated by *quarks* or *gluons* produced in the hard scattering process are $\frac{1}{\sqrt{1}}$ dominated by the differences in these hadron energy fractions indicating that **measurements of the hadron content of jets and improved tuning** of hadronization models can result in an improvement in the precision $\frac{1}{\sqrt{1-\frac{1$ of the knowledge of the ATLAS jet energy scale. The dependence of the ATLAS jet energy measurement on the modelling investigated. **It is found that the hadronic jet response, i.e. the ratio of** the reconstructed jet energy to the true jet energy, varies by $\sim 1-2\%$ **depending on the hadronisation model used in the simulation. This effect is mainly due to differences in the average energy carried by**

Work in Progress: **Strangeness Enhancement from Close-Packing** ness Enhancement Strangene ness Enhancement

Idea: each string exists in an effective background produced by the others

Close-packing Close-packing

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J. Altmann Monash University

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Slide adapted from J. Altmann

Thorny Issue ⚠ The **Proton-to-Pion** Ratio hanism for diquark production

40

Slide adapted from J. Altmann

Confront with Measurements: Strangeness

42

