# Monte Carlo Event Generators

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Australian Government

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### Overview

**General Introduction:** Principles of MC Generators **Event Simulation 1** Hadronization > Dynamics of Confinement Hadronic (pp, pA, AA) Collisions > "Collective Phenomena" New Discoveries > New Ideas

# 2

### **Event Simulation 2**

Perturbative Aspects  $\leftrightarrow$  Amplitude Calculations Perturbative Uncertainties

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The objective of science

# Measure the measurable, and make the unmeasurable measurable.

It seems there is some doubt whether Galileo actually said this.

# What has philosophy got to do with measuring anything?

Galileo, Concerning the New Star (1606)

(It's the mathematicians you have to trust, and they measure the skies like we measure a field.)

### Do measurements ⇔ Learn about Nature



### Elementary Fields & Parameters Lagrangians & QFT Perturbation Theory

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# ↔ Experiment

(Typically) Very Large Backgrounds

Detector Signals Reconstructions # of Observed Events

### Do measurements ⇔ Learn about Nature



### Need **precise** and **detailed** relations + Lots of **interesting physics** on the way

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# ↔ Experiment

(Typically) Very Large Backgrounds

# Connecting theory and experiment

# **MC Event Generators**



HARD-PROCESS SKELETONS: Example:  $gg \to t\bar{t}$ + Resonance decays

+ RADIATIVE CORRECTIONS + MPI + CR + HADRONISATION, ... + HADRON (&  $\tau$ ) DECAYS

eeeeeeeeeeee

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+ DETECTOR SIMULATIONS + TRIGGERS + RECONSTRUCTION

 $\Rightarrow$  Physics Analysis

• • •

MPI

# Foundational Principles of MC Event Generators

# 1. Divide and Conquer

Split the problem into (many) simpler pieces

# 2. Knowledge is Power

The simpler pieces are given by Mathematical Factorisations

+ The loss of perturbation theory in the nonperturbative regime does not imply a total loss of predictivity!

# 3. God plays dice

We'll do the same!

# 1 — Divide et Impera

Hard LHC collisions contain 100s of particles Need (differential)  $\sigma_{pp}$  for that number of "legs"

# Help! Some of them are hadrons! — Non-perturbative

And/or have small opening angles

And/or are "soft"

+ Phase Space  $\propto \prod_{i=1}^{100} \frac{d^3 p_i}{2E_i}$ 

### How would you:

Construct, square, and integrate 100-leg amplitudes (with a lot of IRdivergent + non-pert. structure) over 300-dimensional phase spaces?

### break it down!

### Perturbative Infinities

### 2 — Scientia Potentia Est

Some Important Factorisations:

- **Factorisation of Long-Distance QCD**  $\implies$  Can use Perturbation Theory Narrow-Width Limit  $\implies$  Resonance & Hadron production and decay Soft and Collinear Factorisation in Gauge Theories  $\implies$  Iterative FSR & ISR
- + Well-Designed Observables E.g., IR-safe & -sensitive, ratios vs yields, etc.
- Give data to ML and let it work out the transfer function(s)? If the algorithm misses any of the factorisations (or conservations laws), would you trust it? In principle, the data contains the laws. But features differ by orders of magnitude, many are quasi-fractal, ... In MCEGs, some laws may of course also be implemented imperfectly But physical basis can be discussed, learned from, and in principle systematically improved How to use ML for interpretation? For us to learn. What are we looking at?

### 3 — Most gods play dice; Fate plays chess. Pratchett

Physics

Separation of time scales > Factorizations

→ Can split big problem into many (nested) pieces + make random choices (MC)<sup>2</sup> ~ like in nature

 $\mathcal{P}_{\mathrm{event}} = \mathcal{P}_{\mathrm{hard}} \otimes \mathcal{P}_{\mathrm{dec}} \otimes \mathcal{P}_{\mathrm{ISR}} \otimes \mathcal{P}_{\mathrm{FSR}} \otimes \mathcal{P}_{\mathrm{MPI}} \otimes \mathcal{P}_{\mathrm{Had}} \otimes \dots$ 



### Hard Process & Decays:

Use process-specific (N)LO matrix elements (e.g.,  $gg \to H^0 \to \gamma\gamma)$  $\rightarrow$  Sets "hard" resolution scale for process:  $Q_{HARD}$ 

### ISR & FSR (Initial- & Final-State Radiation):

function of resolution scale; from  $Q_{HARD}$  to  $Q_{HAD} \sim 1 \text{ GeV}$ 

### MPI (Multi-Parton Interactions)

### Hadronisation

Strings or clusters; followed by hadron and  $\tau$  decays



Driven by differential (e.g., DGLAP) evolution equations,  $dP/dQ^2$ , as

- Protons contain lots of partons  $\rightarrow$  can have additional (soft) parton-parton interactions  $\rightarrow$  Additional (soft) "Underlying-Event" activity
- Nonperturbative modeling of partons → hadrons transition

# The Physics of Event Generators

- O Hard Interaction
- Resonance Decays
- MECs, Matching & Merging
- FSR
- ISR\*
- QED
- Weak Showers
- Hard Onium
- Multiparton Interactions
- Beam Remnants\*
- Strings
- Ministrings / Clusters
- Colour Reconnections
- String Interactions
- Bose-Einstein & Fermi-Dirac
- Primary Hadrons
- Secondary Hadrons
- Hadronic Reinteractions
- (\*: incoming lines are crossed)





# The Physics of Event Generators





# Confine ments in thigh energy collisions

In high-energy processes, need a dynamical process to ensure partons (quarks and gluons) become **confined** within hadrons

i.e. a non-perturbative parton → hadron map

**Model requirements** > Colour neutralisation > Dynamical mapping to on-shell hadrons



 $pp \rightarrow t\bar{t}$ 

### Requirement #1: Colour Neutralisation

The point of confinement is that partons are **coloured** A physical model needs two or more partons to create colour-neutral objects

On lattice, compute **potential energy** V(R) of a **colour-singlet**  $q\bar{q}$  **state** as function of the distance, R, between the q and  $\bar{q}$ :



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 $F(r) \simeq \text{const} = \kappa \simeq 1 \text{ GeV}/\text{fm} \iff V(r) \simeq \kappa r$ 

### COIUUI Incuransation Strings!!



### High separation energies $\gtrsim$ 1 GeV $\implies$ String Breaks (by pair creation):



Modelled by analogy with "Schwinger Mechanism" in QED

→ Gaussian suppression with "transverse mass": exp

### model the colour confinement field as a string

# $\succ$ Strings form between partons that form overall

# Who gets confined with whom?



A corresponding event record from PYTHIA, up to the second gluon emission

#	id	name	status	mothers	daughters	colours	p_x	p_y	p_z	е	m
5	23	(ZO)	-22	3 4	6 7		0.000	0.000	0.000	91.188	91.188
6	3	(s)	-23	5 0	10 0	101 0	-12.368	16.523	40.655	45.594	0.000
7	-3	(sbar)	-23	5 0	89	0 101	12.368	-16.523	-40.655	45.594	0.000
8	21	(g)	-51	7 0	13 0	103 101	9.243	-9.146	-29.531	32.267	0.000
9	-3	sbar	51	7 0		0 103	3.084	-7.261	-10.973	13.514	0.000
10	3	(s)	-52	6 0	11 12	101 0	-12.327	16.406	40.505	45.406	0.000
11	21	g	-51	10 0		101 102	-2.834	-2.408	1.078	3.872	0.000
12	3	S	51	10 0		102 0	-10.246	17.034	38.106	42.979	0.000
13	21	g	52	8 0		103 101	9.996	-7.366	-28.211	30.823	0.000

## Requirement #2: on-shell hadrons

**Observation:** All string breaks are **causally disconnected** ( $\geq$  independent modulo entanglement from common origin)



"Left-right symmetry"  $\implies$  FF constrained to a form with **two free parameters**, **a** & **b** (constrained by fits to measured hadron spectra)

[See, e.g., <u>Amoroso et al., JCAP 05 (2019) 007</u>]

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- Lorentz invariance  $\implies$  string breaks can be considered in any order.
- Exploit this to split off "outermost" hadron either from left or right (randomly) — **iteratively!**
- Hadron h takes a fraction z of the quark momentum
- **Probability distribution** in  $z \in [0,1]$  parametrised by Fragmentation Function,  $f_{Lund}(z, Q_{HAD}^2)$

 $f_{\text{Lund}}(z) \propto \frac{1}{z} (1-z)^a \exp\left(-\frac{b(m_h^2 + p_{\perp h}^2)}{t}\right)$ 

Supresses high z

## Gluon Kinks: The Signature Feature of the Lund Model



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### Alternative: The Cluster Model — Used in HERWIG & SHERPA

### **Alternative to strings:**



## Hadron Collisions $\rightarrow$ Multi-Parton Interactions

### **Protons are composite**

### **One** proton = **beam** of partons

 $+ d\sigma_{parton-parton}$  is dominated by *t*-channel gluon exchange: **diverges for**  $\hat{p}_{\perp} \rightarrow 0$  GeV

 $\propto \frac{\alpha_s(p_\perp)}{t}$ 



 $\begin{array}{l} \text{Interpretation:} & \frac{\sigma_{\mathsf{parton-parton}}(\hat{p}_{\perp})}{\sigma_{\mathsf{hadron-hadron}}} \sim \left< n \right>_{\mathrm{parton-parton}}(\hat{p}_{\perp}) \end{array}$ 

(Regulated at low  $\hat{p}_{\perp}$  by IR cutoff ~ colour screening)

→ Multiple Parton-Parton Interactions (MPI)

α\_=0.135 CTEQ6L1



### $\approx$ poor man's saturation

### ↔ cut pomerons in Regge Theory



# **A Brief History of MPI** (in PYTHIA)

**1987** [Sjöstrand & van Zijl, Phys.Rev.D 36 (1987) 2019]

Cast MPI as Sudakov-style evolution:

Analogous to  $\sigma_{X+jet}(p_{\perp})/\sigma_X$  for parton showers



with Impact-parameter dependence



Crucial to describe "Underlying Event"

# Pythia 8 — Interleaved Evolution

2005 [Sjöstrand & PS, Eur.Phys.J.C 39 (2005) 129] Interleave MPI & ISR evolutions in one common sequence of p<sub>T</sub> → ISR & MPI "compete" for the available x in the proton remnant. 2011 [Corke & Sjöstrand, JHEP 03 (2011) 032] Also include **FSR** in interleaving

~ Fine-graining of all event structure above hadronization scale in one common sequence of quantum mechanical resolution  $\propto p_{\perp}$ 



# Confinement in *pp* Collisions

MPI or cut pomerons  $\Rightarrow$  lots of coloured partons scattered into final state Who gets confined with whom?

Each has a colour ambiguity ~  $1/N_C^2$  ~ 10%

- E.g.: random triplet charge has 1/9 chance to be in **singlet** state with **random antitriplet**:
  - $3 \otimes \overline{3} = 8 \oplus 1$ ,
  - $3 \otimes 8 = 15 + 6 + 3$ , etc.

(CR) more likely than not

Expect Prob(no CR)  $\propto \left(1 - \frac{1}{N_C^2}\right)^2$ 

(And do other things happen? Emergent dynamics?)

\*): in this context, QCD CR simply refers to an ambiguity beyond Leading  $N_c$ , known to exist. The term "CR" can also be used more broadly.



### "Parton Level" (Event structure before confinement)

## String-length minimisation and $\langle PT \rangle (N_{ch})$

When many string configurations are possible, assume nature picks the one with smallest potential energy ~ "string length"



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[See also Ortiz et al., Phys.Rev.Lett. 111 (2013) 4, 042001]

# QCD @ LHC $\succ$ Lots of New Discoveries!



Regard tension *k* as an emergent quantity (not fundamental strings)

May depend on (invariant) time  $\tau$ ? E.g., hot strings which cool down [Hunt-Smith & PZS EPJ C 80 (2020) 11]



May depend on environment? (e.g., other strings nearby) Two approaches (so far) within Lund string-model context: **Colour Ropes** [Bierlich et al. 2015] + several more recent **Close-Packing** [Fischer & Sjöstrand 2017] + Work in progress with L. Bernardinis & V. Zaccolo (Trieste)

### Cyclonic and Anticyclonic Winds



### Non-Linear String Dynamics? Id ICE



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## What about Baryon Number?

### Types of string topologies:



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# Fragmentation of String Junctions

Assume Junction Strings have same properties as ordinary ones (u:d:s, Schwinger  $p_T$ , etc) > No new string-fragmentation parameters



[Sjöstrand & PS, <u>NPB 659 (2003) 243</u>] [+ Altmann & PS, JHEP 07 (2024) 238]

The Junction Baryon is the most "subleading" hadron in all three "jets".

Generic prediction: low pt

A Smoking Gun for String Junctions: Baryon enhancements at low  $p_T$ 

# Colour Reconnections

### [Christiansen & PS 2015, Altmann & PS 2024]





**Next Steps:** put it all together (+ "Altmann mechanism" for diquark disruption in octet fields) See how close we can get to describing light, strange, and heavy-flavour mesons + baryons in pp + Lund group developing extensions/applications to heavy-ion collisions!

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## Heavy-Ion Physics

### **Disclaimer:** I am not an expert

- Also for HI, there are of course event generators + E.g., ANGANTYR, EPOS, HIJING, JEWEL, QGSJET, SIBYLL, ...
- Another big class of models: statistical hadronization
- Differ in how much detail you aim for, how multi-differential and/or eventby-event you want to be able to go ...
- You may **want** to focus on macroscopic properties, not the microphysics
- Or you may **want** to pursue a microscopic description, without all macroscopic aspects
- Most of us specialise, but I don't think the point is to pick a winner As a physicist, I'd like to understand **both:** what are the **macroscopic** properties? what is the microphysics? How do the former emerge from the latter? Which paradigms are compatible / incompatible? How to form **clear** conclusions from **data?**

Lots of recent activity ! Also in PYTHIA Led by Jyväskylä & Lund

## Beyond Strings — QGP?

Currently most realistic complete approach for pp  $\leftrightarrow$  pA  $\leftrightarrow$  AA? The core-corona solution [Werner 2007]: mix discrete strings with continuous QGP



### core => hydro => statistical decay ( $\mu = 0$ ) corona => string decay

Allows smooth transition between string and hydro descriptions. Implemented in **EPOS MC** Qualitatively agrees with ALICE strangeness data (but too steep rise with multiplicity?)



## **Conversely:** Collective flow from strings? (without QGP)

Colour-electric fields -> Classical force



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# Pythia for Cosmic Rays $\leftrightarrow$ Corsika 8



with Applications to Cosmic Rays",

- Models arbitrary hadron-hadron collisions at low energies.
- Models arbitrary hadron-p/n collisions at any energy.
- Initialization slow,  $\sim 15$  minutes,  $\star$  but thereafter works for any hadron-p/n at any energy, and \* initialization data can be saved, so only need to do once.
- The ANGANTYR nuclear geometry part used to extend to hadron-nucleus at any energy.
- Native C++ simplifies interfacing PYTHIA  $8 \leftrightarrow \text{CORSIKA } 8$ . So far limited comparisons with data.

### Based on 2 articles by **Marius Utheim** & TS:

- "A Framework for Hadronic Rescattering in pp Collisions", Eur. Phys. J. C80 (2020) 907, arXiv:2005.05658
- "Hadron Interactions for Arbitrary Energies and Species,
- Eur. Phys. J. C82 (2022) 21, arXiv:2108.03481

### + Extension with ANGANTYR (→incoming nuclei) > PYTHIA 8.313

# Extra Slides

# (Note on the Length of Strings)

### In Spacetime:

String tension  $\approx$  1 GeV/fm  $\rightarrow$  a 50-GeV quark can travel 50 fm before all its kinetic energy is transformed to potential energy in the string. Then it must start moving the other way.

 $(\rightarrow$  "yo-yo" model of mesons. Note: string breaks  $\rightarrow$  several mesons)

The MC implementation is formulated in momentum space Lightcone momenta  $p_{\pm} = E \pm p_z$  along string axis  $\rightarrow$  Rapidity (along string axis) and  $p_{\perp}$  transverse to it  $y = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) = \frac{1}{2} \ln \left( \frac{(E + p_z)^2}{E^2 - p_z^2} \right) \qquad \Longrightarrow \qquad y_{\max} \sim \ln \left( \frac{2E_q}{m_{\pi}} \right)$ 

### **Particle Production:** Scaling in $z \implies$ flat in rapidity (long. boost invariance) "Lightcone scaling"



 $\langle n_{\rm ch} \rangle \approx c_0 + c_1 \ln E_{\rm cm}$ , ~ Poissonian multiplicity distribution

## Particle Composition: Impact on Jet Energy Scale



### ATLAS PUB Note

ATL-PHYS-PUB-2022-021

29th April 2022



### Dependence of the Jet Energy Scale on the Particle Content of Hadronic Jets in the ATLAS Detector Simulation

The dependence of the ATLAS jet energy measurement on the modelling in Monte Carlo simulations of the particle types and spectra within jets is investigated. It is found that the hadronic jet response, i.e. the ratio of the reconstructed jet energy to the true jet energy, varies by  $\sim 1-2\%$ depending on the hadronisation model used in the simulation. This effect is mainly due to differences in the average energy carried by kaons and baryons in the jet. Model differences observed for jets initiated by *quarks* or *gluons* produced in the hard scattering process are dominated by the differences in these hadron energy fractions indicating that measurements of the hadron content of jets and improved tuning of hadronization models can result in an improvement in the precision of the knowledge of the ATLAS jet energy scale.

- Variation largest for gluon jets For  $E_T = [30, 100, 200] \text{ GeV}$ Max JES variation = [3%, 2%, 1.2%]
- Fraction of jet  $E_T$  carried by baryons (and kaons) varies significantly
  - Reweighting to force similar baryon and kaon fractions
  - Max variation → [1.2%, 0.8%, 0.5%]
  - Significant potential for improved Jet Energy Scale uncertainties!
- Motivates Careful Models & Careful Constraints
  - Interplay with advanced UE models
  - In-situ constraints from LHC data
  - Revisit comparisons to LEP data

# Work in Progress: Strangeness Enhancement from Close-Packing

Idea: each string exists in an effective background produced by the others

### Close-packing



Dense string environments



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Slide adapted from J. Altmann

# Thorny Issue 🤔 The Proton-to-Pion Ratio



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Slide adapted from J. Altmann

### Confront with Measurements: Strangeness



